

*Precision Cosmology with
Large-Scale Structure Surveys*

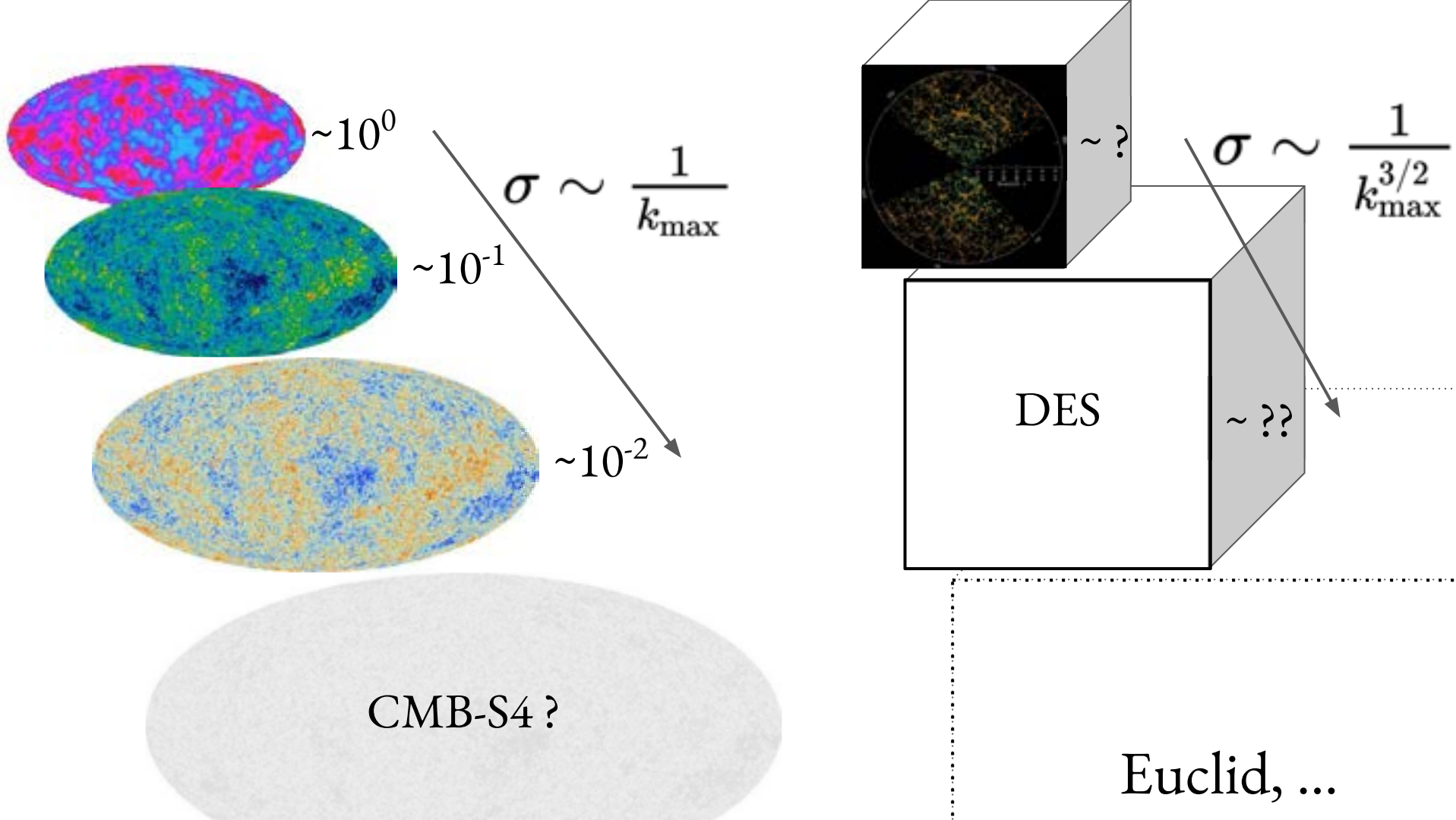
*The Effective Field Theory
of Large-Scale Structure
applied to SDSS-BOSS data*

April, 26th, 2019

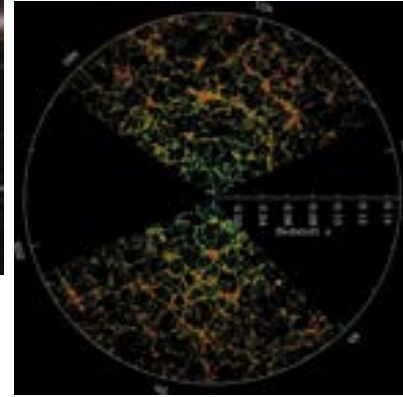
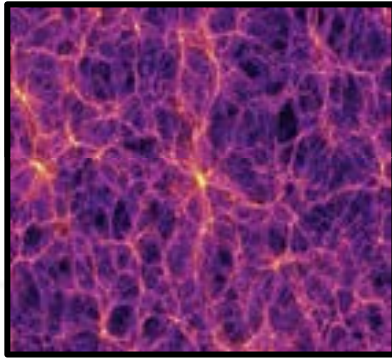
@2019 CCNU - cfa @USTC Junior Cosmology Symposium

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The EFTofLSS program



$\zeta(\mathbf{x})$

Perturbation theory,
N-body simulations

$\delta(\mathbf{x})$

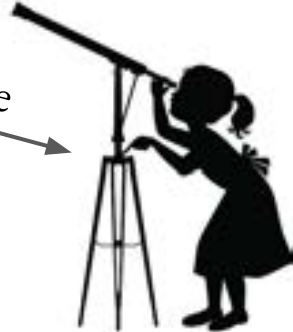
Tracers biases

$\delta_g(\mathbf{x})$

Redshift space
distortions

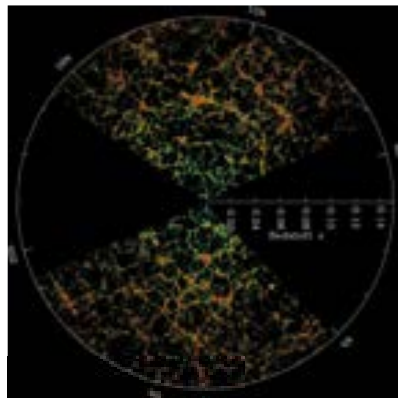
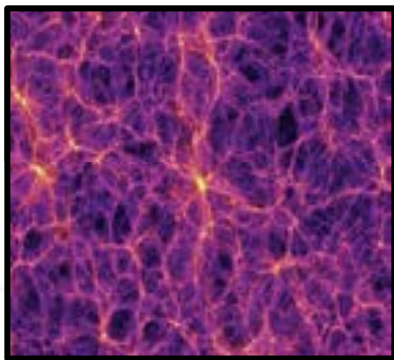
$\delta_g(z)$

Time



The EFTofLSS program

- Slide inspired from a talk of E. Pajer



$\zeta(\mathbf{x})$

Perturbation theory,
N-body simulations

$\delta(\mathbf{x})$

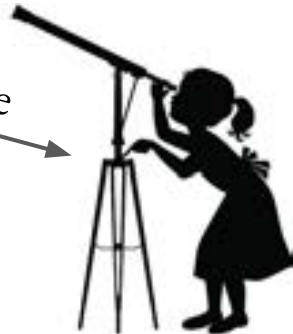
Tracers biases

$\delta_g(\mathbf{x})$

Redshift space
distortions

$\delta_g(z)$

Time



Cosmology recipe

Start with vanilla: Λ CDM

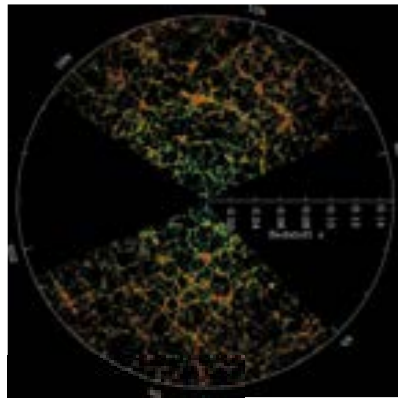
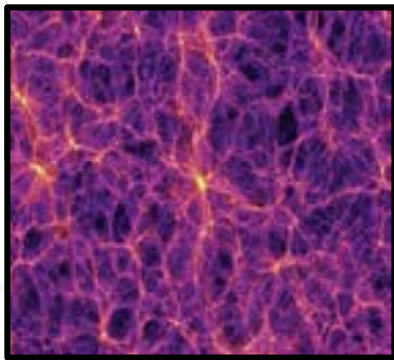
Evolve the fields δ , v ...

Add biasing and redshift space distortions

Compute correlation functions

Compare with observations

“Cosmology in one slide”
slide inspired from a talk of E. Pajer



$\zeta(\mathbf{x})$

Perturbation theory,
N-body simulations

$\delta(\mathbf{x})$

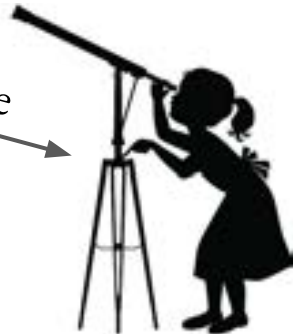
Tracers biases

$\delta_g(\mathbf{x})$

Redshift space
distortions

$\delta_g(z)$

Time



Cosmology recipe

Start with vanilla: Λ CDM

Evolve the fields $\delta, v \dots$

Add biasing and redshift space distortions

Compute correlation functions

Compare with observations

Start over with your favorite ingredients: f_{NL} , warm DM, ~~GR~~ ...

I. EFTofLSS “ Effective Field Theory of Large-Scale Structure ”

Building LSS observables from first principles

II. Redshift Surveys Data Analysis

Extracting cosmological information from LSS

III. Results

SDSS-BOSS data analysis results

with G. d'Amico, J. Gleyzes, N. Kokron, D. Markovic, L. Senatore,
F. Beutler, H. Gil Marin

I. EFTofLSS

Building LSS observables from first principles

EFTofLSS and Dielectric Materials

slide inspired from a talk of L. Senatore

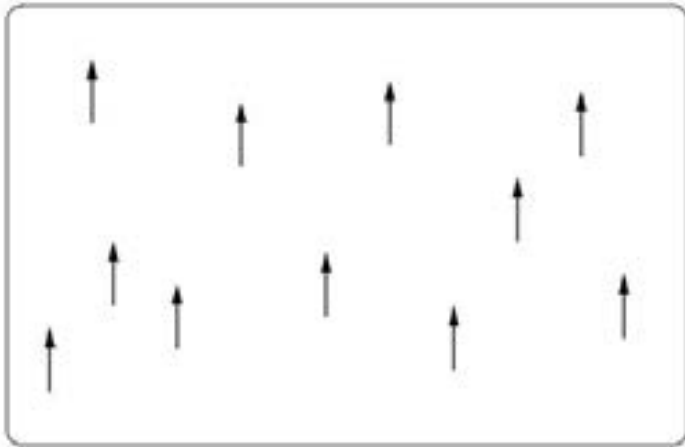
Dielectric Materials Theory:

massless spin-1 object (light) interacting with composite objects (atoms)

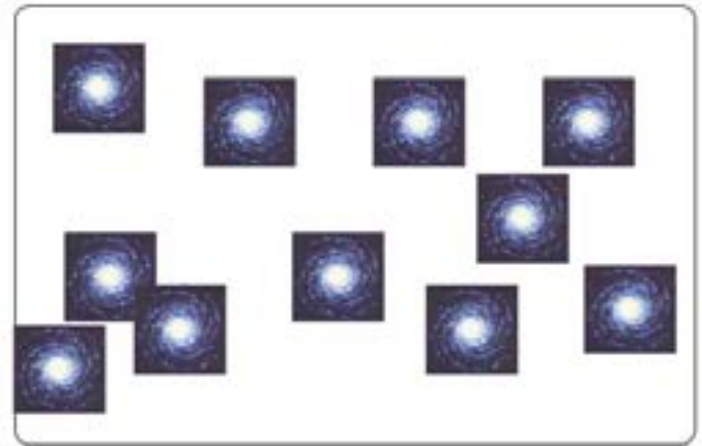
EFTofLSS:

massless spin-2 object (gravity) interacting with composite objects (galaxies)

Dielectric Fluid



Dielectric Fluid



One slide of equations

$$\dot{\delta}_\ell + \frac{1}{a} \partial_i ((1 + \delta_\ell) v_\ell^i) = 0 ,$$

Dark matter

$$\dot{v}_\ell^i + H v_\ell^i + \frac{1}{a} v_\ell^j \partial_j v_\ell^i + \frac{1}{a} \partial_i \phi_\ell = \int^t dt' [c_{s,1}(t, t') \delta_\ell(x_\text{fl}(\vec{x}, t, t'), t') \\ + c_{s,2}(t, t') \delta_\ell(x_\text{fl}(\vec{x}, t, t'), t')^2 + \dots]$$

Energy + momentum conservation equations in Newton gravity
for the long-wavelength modes (most general parametric form)

One slide of equations

Solved perturbatively with a *finite* number of *counterterms* at each perturbative *order*

$$\dot{\delta}_\ell + \frac{1}{a} \partial_i ((1 + \delta_\ell) v_\ell^i) = 0 ,$$

Dark matter

$$\delta_\ell(\vec{k}, t) = \sum_n \delta_\ell^{(n)}(\vec{k}, t)$$

$$\begin{aligned} \dot{v}_\ell^i + H v_\ell^i + \frac{1}{a} v_\ell^j \partial_j v_\ell^i + \frac{1}{a} \partial_i \phi_\ell = \int^{t'} dt' [c_{s,1}(t, t') \delta_\ell(x_\text{fl}(\vec{x}, t, t'), t') \\ + c_{s,2}(t, t') \delta_\ell(x_\text{fl}(\vec{x}, t, t'), t')^2 + \dots] \end{aligned}$$

One slide of equations

$$\dot{\delta}_\ell + \frac{1}{a} \partial_i ((1 + \delta_\ell) v_\ell^i) = 0 ,$$

Dark matter

$$\delta_\ell(\vec{k}, t) = \sum_n \delta_\ell^{(n)}(\vec{k}, t)$$

$$\dot{v}_\ell^i + H v_\ell^i + \frac{1}{a} v_\ell^j \partial_j v_\ell^i + \frac{1}{a} \partial_i \phi_\ell = \int^t dt' [c_{s,1}(t, t') \delta_\ell(x_\text{fl}(\vec{x}, t, t'), t') \\ + c_{s,2}(t, t') \delta_\ell(x_\text{fl}(\vec{x}, t, t'), t')^2 + \dots]$$

$$\delta_{\ell,g}(\vec{x}, t) = \int^t dt' [\bar{c}_1(t, t') \delta_\ell(x_\text{fl}(\vec{x}, t, t'), t')$$

Galaxies

$$+ \bar{c}_2(t, t') \partial_i v_\ell^i(x_\text{fl}(\vec{x}, t, t'), t')^2 + \bar{c}_3(t, t') \delta_\ell(x_\text{fl}(\vec{x}, t, t'), t')^2 + \dots]$$

Expressed as coefficient-weighted combinations of the underlying DM

One slide of equations

$$\dot{\delta}_\ell + \frac{1}{a} \partial_i ((1 + \delta_\ell)) v_\ell^i = 0 ,$$

Dark matter

$$\delta_\ell(\vec{k}, t) = \sum_n \delta_\ell^{(n)}(\vec{k}, t)$$

$$\dot{v}_\ell^i + H v_\ell^i + \frac{1}{a} v_\ell^j \partial_j v_\ell^i + \frac{1}{a} \partial_i \phi_\ell = \int dt' [c_{s,1}(t, t') \delta_\ell(x_\text{fl}(\vec{x}, t, t'), t') + c_{s,2}(t, t') \delta_\ell(x_\text{fl}(\vec{x}, t, t'), t')^2 + \dots]$$

$$\delta_{\ell,g}(\vec{x}, t) = \int dt' [\bar{c}_1(t, t') \delta_\ell(x_\text{fl}(\vec{x}, t, t'), t') + \bar{c}_2(t, t') \partial_i v_\ell^i(x_\text{fl}(\vec{x}, t, t'), t')^2 + \bar{c}_3(t, t') \delta_\ell(x_\text{fl}(\vec{x}, t, t'), t')^2 + \dots]$$

Galaxies

Expressed as coefficient-weighted combinations of the underlying DM

$$\delta_{\ell,g,r}(\vec{k}, t) = \delta_{\ell,g}(\vec{k}, t) - i \frac{k_z}{aH} v_{\ell,g}^z(\vec{k}, t) + \frac{i^2}{2} \left(\frac{k_z}{aH} \right)^2 [v_{\ell,g}^z(\vec{x}, t)^2]_{\vec{k}}$$

Galaxies

$$- \frac{i^3}{3!} \left(\frac{k_z}{aH} \right)^3 [v_{\ell,g}^z(\vec{x}, t)^3]_{\vec{k}} - i \frac{k_z}{aH} [v_{\ell,g}^z(\vec{x}, t) \delta(\vec{x}, t)]_{\vec{k}} + \frac{i^2}{2} \left(\frac{k_z}{aH} \right)^2 [v_{\ell,g}^z(\vec{x}, t)^2 \delta_{\ell,g}(\vec{x}, t)]_{\vec{k}} +$$

**in
Redshift**

$$+ \int dt' \left(\frac{aH}{k_{\text{NL}}} \right)^2 \left[c_{r,1}(t, t') \delta_D^{(3)}(\vec{k}) + \left(c_{r,2}(t, t') + c_{r,3}(t, t') \frac{k_z^2}{k^2} \right) [\delta_\ell(x_\text{fl}(\vec{x}, t, t'), t')]_{\vec{k}} \right] +$$

Space

One slide of equations

$$\dot{\delta}_\ell + \frac{1}{a} \partial_i ((1 + \delta_\ell) v_\ell^i) = 0, \quad \text{Dark matter} \quad \delta_\ell(\vec{k}, t) = \sum_n \delta_\ell^{(n)}(\vec{k}, t)$$

$$\dot{v}_\ell^i + H v_\ell^i + \frac{1}{a} v_\ell^j \partial_j v_\ell^i + \frac{1}{a} \partial_i \phi_\ell = \int^t dt' [c_{s,1}(t, t') \delta_\ell(x_\text{fl}(\vec{x}, t, t'), t') \\ + c_{s,2}(t, t') \delta_\ell(x_\text{fl}(\vec{x}, t, t'), t')^2 + \dots]$$

$$\delta_{\ell,g}(\vec{x}, t) = \int^t dt' [\bar{c}_1(t, t') \delta_\ell(x_\text{fl}(\vec{x}, t, t'), t') \\ + \bar{c}_2(t, t') \partial_i v_\ell^i(x_\text{fl}(\vec{x}, t, t'), t')^2 + \bar{c}_3(t, t') \delta_\ell(x_\text{fl}(\vec{x}, t, t'), t')^2 + \dots] \quad \text{Galaxies}$$

$$\delta_{\ell,g,r}(\vec{k}, t) = \delta_{\ell,g}(\vec{k}, t) - i \frac{k_z}{aH} v_{\ell,g}^z(\vec{k}, t) + \frac{i^2}{2} \left(\frac{k_z}{aH} \right)^2 [v_{\ell,g}^z(\vec{x}, t)^2]_{\vec{k}} \\ - \frac{i^3}{3!} \left(\frac{k_z}{aH} \right)^3 [v_{\ell,g}^z(\vec{x}, t)^3]_{\vec{k}} - i \frac{k_z}{aH} [v_{\ell,g}^z(\vec{x}, t) \delta(\vec{x}, t)]_{\vec{k}} + \frac{i^2}{2} \left(\frac{k_z}{aH} \right)^2 [v_{\ell,g}^z(\vec{x}, t)^2 \delta_{\ell,g}(\vec{x}, t)]_{\vec{k}} + \\ + \int dt' \left(\frac{aH}{k_{\text{NL}}} \right)^2 \left[c_{r,1}(t, t') \delta_D^{(3)}(\vec{k}) + \left(c_{r,2}(t, t') + c_{r,3}(t, t') \frac{k_z^2}{k^2} \right) [\delta_\ell(x_\text{fl}(\vec{x}, t, t'), t')]_{\vec{k}} \right] + \text{Space}$$

Galaxies
in
Redshift
Space

One slide of equations

$$\dot{\delta}_\ell + \frac{1}{a} \partial_i ((1 + \delta_\ell) v_\ell^i) = 0, \quad \delta_\ell(\vec{k}, t) = \sum_n \delta_\ell^{(n)}(\vec{k}, t)$$

$$\dot{v}_\ell^i + H v_\ell^i + \frac{1}{a} \partial_j v_\ell^j v_\ell^i + \frac{1}{a} \partial_i \phi_\ell = \int^t dt' [c_{s,1}(t, t') \delta_\ell(x_{\text{fl}}(\vec{x}, t, t'), t') + c_{s,2}(t, t') \delta_\ell(x_{\text{fl}}(\vec{x}, t, t'), t')^2 + \dots]$$

$$\delta_{\ell,g}(\vec{x}, t) = \int dt' [\bar{c}_1(t, t') \delta_\ell(x_{\text{fl}}(\vec{x}, t, t'), t') + \bar{c}_2(t, t') \partial_i v_\ell^i(x_{\text{fl}}(\vec{x}, t, t'), t')^2 + \bar{c}_3(t, t') \delta_\ell(x_{\text{fl}}(\vec{x}, t, t'), t')^2 + \dots]$$

= Linear (bias-weighted) combination of

$$\delta_{\ell,g,r}(\vec{k}, t) = \delta_{\ell,g}(\vec{k}, t) - i \frac{k_z}{aH} [v_{\ell,g}^z(\vec{x}, t) \delta(\vec{x}, t)]_{\vec{k}} + \frac{i^2}{2} \left(\frac{k_z}{aH} \right)^2 [v_{\ell,g}^z(\vec{x}, t)^2 \delta_{\ell,g}(\vec{x}, t)]_{\vec{k}} + \dots$$

DM correlation functions

$$- \frac{i^3}{3!} \left(\frac{k_z}{aH} \right)^3 [v_{\ell,g}^z(\vec{x}, t)^3]_{\vec{k}} - i \frac{k_z}{aH} [v_{\ell,g}^z(\vec{x}, t) \delta(\vec{x}, t)]_{\vec{k}} + \frac{i^2}{2} \left(\frac{k_z}{aH} \right)^2 [v_{\ell,g}^z(\vec{x}, t)^2 \delta_{\ell,g}(\vec{x}, t)]_{\vec{k}} + \dots$$

$$+ \int dt' \left(\frac{aH}{k_{\text{NL}}} \right)^2 \left[c_{r,1}(t, t') \delta_D^{(3)}(\vec{k}) + \left(c_{r,2}(t, t') + c_{r,3}(t, t') \frac{k_z^2}{k^2} \right) [\delta_\ell(x_{\text{fl}}(\vec{x}, t, t'), t')]_{\vec{k}} \right] + \dots$$

Bottom line:

Correlation functions of galaxies in redshift space

= Linear (bias-weighted) combination of

DM correlation functions

+ Finite number of counterterms

EFTofLSS observables

Galaxies power spectrum in redshift space:

$$\begin{aligned} P_g(k, \mu) &= Z_1(\mu)^2 P_{11}(k) \\ &+ 2 \int d^3q Z_2(\mathbf{q}, \mathbf{k} - \mathbf{q}, \mu)^2 P_{11}(|\mathbf{k} - \mathbf{q}|) P_{11}(q) + 6Z_1(\mu) P_{11}(k) \int d^3q Z_3(\mathbf{q}, -\mathbf{q}, \mathbf{k}, \mu) P_{11}(q) \\ &+ 2Z_1(\mu) P_{11}(k) \left(c_{\text{ct}} \frac{k^2}{k_M^2} + c_{r,1} \mu^2 \frac{k^2}{k_M^2} + c_{r,2} \mu^4 \frac{k^2}{k_M^2} \right) + \frac{1}{\bar{n}_g} \left(c_{\epsilon,1} + c_{\epsilon,2} \frac{k^2}{k_M^2} + c_{\epsilon,3} f \mu^2 \frac{k^2}{k_M^2} \right). \end{aligned}$$

EFTofLSS observables

Galaxies power spectrum in redshift space:

linear power spectrum

$$\begin{aligned}
 P_g(k, \mu) = & \underline{Z_1(\mu)^2 P_{11}(k)} \\
 & + 2 \int d^3q Z_2(\mathbf{q}, \mathbf{k} - \mathbf{q}, \mu)^2 P_{11}(|\mathbf{k} - \mathbf{q}|) P_{11}(q) + 6Z_1(\mu) P_{11}(k) \int d^3q Z_3(\mathbf{q}, -\mathbf{q}, \mathbf{k}, \mu) P_{11}(q) \\
 & + 2Z_1(\mu) P_{11}(k) \left(c_{\text{ct}} \frac{k^2}{k_M^2} + c_{\tau,1} \mu^2 \frac{k^2}{k_M^2} + c_{\tau,2} \mu^4 \frac{k^2}{k_M^2} \right) + \frac{1}{\bar{n}_g} \left(c_{\epsilon,1} + c_{\epsilon,2} \frac{k^2}{k_M^2} + c_{\epsilon,3} f \mu^2 \frac{k^2}{k_M^2} \right).
 \end{aligned}$$

1-loop

Galaxies kernels in redshift space:

composed of density and velocity kernels

functions of 4 bias parameters at the
1-loop

$$Z_1(\mathbf{q}_1) = K_1(\mathbf{q}_1) + f\mu_1^2 G_1(\mathbf{q}_1) = b_1 + f\mu_1^2, \quad (6)$$

$$Z_2(\mathbf{q}_1, \mathbf{q}_2, \mu) = K_2(\mathbf{q}_1, \mathbf{q}_2) + f\mu_{12}^2 G_2(\mathbf{q}_1, \mathbf{q}_2) + \frac{1}{2} f\mu q \left(\frac{\mu_2}{q_2} G_1(\mathbf{q}_2) Z_1(\mathbf{q}_1) + \text{perm.} \right),$$

$$Z_3(\mathbf{q}_1, \mathbf{q}_2, \mathbf{q}_3, \mu) = K_3(\mathbf{q}_1, \mathbf{q}_2, \mathbf{q}_3) + f\mu_{123}^2 G_3(\mathbf{q}_1, \mathbf{q}_2, \mathbf{q}_3)$$

$$+ \frac{1}{3} f\mu q \left(\frac{\mu_3}{q_3} G_1(\mathbf{q}_3) Z_2(\mathbf{q}_1, \mathbf{q}_2, \mu_{123}) + \frac{\mu_{23}}{q_{23}} G_2(\mathbf{q}_2, \mathbf{q}_3) Z_1(\mathbf{q}_1) + \text{cyc.} \right),$$

where here $\mu = \mathbf{q} \cdot \hat{\mathbf{z}}/q$, $\mathbf{q} = \mathbf{q}_1 + \dots + \mathbf{q}_n$, and $\mu_{i_1 \dots i_n} = \mathbf{q}_{i_1 \dots i_n} \cdot \hat{\mathbf{z}}/q_{i_1 \dots i_n}$, $\mathbf{q}_{i_1 \dots i_m} = \mathbf{q}_{i_1} + \dots + \mathbf{q}_{i_m}$

EFTofLSS observables

Galaxies power spectrum in redshift space:

linear power spectrum

$$P_g(k, \mu) = \underbrace{Z_1(\mu)^2 P_{11}(k)}_{\text{1-loop}} + \underbrace{2 \int d^3q Z_2(\mathbf{q}, \mathbf{k} - \mathbf{q}, \mu)^2 P_{11}(|\mathbf{k} - \mathbf{q}|) P_{11}(q) + 6Z_1(\mu) P_{11}(k) \int d^3q Z_3(\mathbf{q}, -\mathbf{q}, \mathbf{k}, \mu) P_{11}(q)}_{\text{1-loop}} + \underbrace{2Z_1(\mu) P_{11}(k) \left(c_{\text{ct}} \frac{k^2}{k_M^2} + c_{r,1} \mu^2 \frac{k^2}{k_M^2} + c_{r,2} \mu^4 \frac{k^2}{k_M^2} \right)}_{\text{counterterms}} + \frac{1}{\bar{n}_g} \left(c_{\epsilon,1} + c_{\epsilon,2} \frac{k^2}{k_M^2} + c_{\epsilon,3} f \mu^2 \frac{k^2}{k_M^2} \right).$$

EFTofLSS observables

Galaxies power spectrum in redshift space:

linear power spectrum

$$\begin{aligned}
 P_g(k, \mu) = & \underbrace{Z_1(\mu)^2 P_{11}(k)}_{\text{1-loop}} \\
 & + 2 \int d^3q Z_2(\mathbf{q}, \mathbf{k} - \mathbf{q}, \mu)^2 P_{11}(|\mathbf{k} - \mathbf{q}|) P_{11}(q) + 6Z_1(\mu) P_{11}(k) \int d^3q Z_3(\mathbf{q}, -\mathbf{q}, \mathbf{k}, \mu) P_{11}(q) \\
 & + 2Z_1(\mu) P_{11}(k) \left(c_{\text{ct}} \frac{k^2}{k_M^2} + c_{r,1} \mu^2 \frac{k^2}{k_M^2} + c_{r,2} \mu^4 \frac{k^2}{k_M^2} \right) + \frac{1}{\bar{n}_g} \left(c_{\epsilon,1} + c_{\epsilon,2} \frac{k^2}{k_M^2} + c_{\epsilon,3} f \mu^2 \frac{k^2}{k_M^2} \right).
 \end{aligned}$$

counterterms

1 dark matter counterterm:
Renormalization the 1-loop

2 redshift-space counterterms:
Renormalization of velocity operators

~

Higher derivative term:

Encloses spatial extension of galaxies

EFTofLSS observables

Galaxies power spectrum in redshift space:

linear power spectrum

$$P_g(k, \mu) = \underbrace{Z_1(\mu)^2 P_{11}(k)}_{\text{1-loop}} + \underbrace{2 \int d^3q Z_2(\mathbf{q}, \mathbf{k} - \mathbf{q}, \mu)^2 P_{11}(|\mathbf{k} - \mathbf{q}|) P_{11}(q)}_{\text{1-loop}} + \underbrace{6Z_1(\mu)P_{11}(k) \int d^3q Z_3(\mathbf{q}, -\mathbf{q}, \mathbf{k}, \mu) P_{11}(q)}_{\text{1-loop}} + \underbrace{2Z_1(\mu)P_{11}(k) \left(c_{\text{ct}} \frac{k^2}{k_M^2} + c_{r,1} \mu^2 \frac{k^2}{k_M^2} + c_{r,2} \mu^4 \frac{k^2}{k_M^2} \right)}_{\text{counterterms}} + \underbrace{\frac{1}{\bar{n}_g} \left(c_{\epsilon,1} + c_{\epsilon,2} \frac{k^2}{k_M^2} + c_{\epsilon,3} f \mu^2 \frac{k^2}{k_M^2} \right)}_{\text{stochastic terms}}.$$

Function of 10 free ‘EFT’ parameters:

- 4 galaxies biases
- 3 counterterms
- 3 stochastic terms

II. Redshift Surveys Data Analysis

Extracting cosmological information from LSS

Analysis pipeline

$$\{A_s, \Omega_m, h\}$$

Decomposition in bias-independent parts:

$$P_g(k, z) = \sum_n \mu^{2\alpha_n} f(z)^{\beta_n} b_{i_n}(z)^{\gamma_n} b_{j_n}(z)^{\delta_n} D(z)^{2\rho_n} P_n(k) ,$$

Analysis pipeline

Decomposition in bias-independent parts:

$$P_g(k, z) = \sum_n \mu^{2\alpha_n} f(z)^{\beta_n} b_{i_n}(z)^{\gamma_n} b_{j_n}(z)^{\delta_n} D(z)^{2\rho_n} P_n(k) ,$$

Decomposition in multipoles with Alock-Paszynski effect:

$$P_n^\ell(k^{\text{ref}}) = \frac{2\ell + 1}{2q_{\parallel}q_{\perp}^2} \int_{-1}^1 d\mu^{\text{ref}} \mu(\mu^{\text{ref}})^{2\alpha_n} P_n(k(k^{\text{ref}}, \mu^{\text{ref}})) \mathcal{P}_\ell(\mu^{\text{ref}}) ,$$

$$k = \frac{k^{\text{ref}}}{q_{\perp}} \left[1 + (\mu^{\text{ref}})^2 \left(\frac{1}{F^2} - 1 \right) \right]^{1/2} ,$$
$$\mu = \frac{\mu^{\text{ref}}}{F} \left[1 + (\mu^{\text{ref}})^2 \left(\frac{1}{F^2} - 1 \right) \right]^{-1/2} ,$$
$$q_{\perp} = \frac{D_A(z_{\text{eff}})H(z=0)}{D_A^{\text{ref}}(z_{\text{eff}})H^{\text{ref}}(z=0)} , \quad q_{\parallel} = \frac{H^{\text{ref}}(z_{\text{eff}})/H^{\text{ref}}(z=0)}{H(z_{\text{eff}})/H(z=0)} .$$

where $F = q_{\parallel}/q_{\perp}$.

AP parameters are not free
in our analysis

Analysis pipeline

Decomposition in bias-independent parts:

$$P_g(k, z) = \sum_n \mu^{2\alpha_n} f(z)^{\beta_n} b_{i_n}(z)^{\gamma_n} b_{j_n}(z)^{\delta_n} D(z)^{2\rho_n} P_n(k) ,$$

Decomposition in multipoles with Alock-Paszynski effect:

$$P_n^\ell(k^{\text{ref}}) = \frac{2\ell + 1}{2q_{\parallel}q_{\perp}^2} \int_{-1}^1 d\mu^{\text{ref}} \mu(\mu^{\text{ref}})^{2\alpha_n} P_n(k(k^{\text{ref}}, \mu^{\text{ref}})) \mathcal{P}_\ell(\mu^{\text{ref}}) ,$$

Application of the window functions (in Fourier space):

$$P_\ell^{(\text{EFT})^{(W)}}(k) = W_{\ell,\ell'}(k, k') \cdot P_{\ell'}^{(\text{EFT})}(k) ,$$

$$W(k, k')_{\ell,\ell'} = \frac{2}{\pi} (-i)^\ell i^{\ell'} k'^2 \int ds s^2 j_\ell(ks) Q_{\ell,\ell'}(s) \cdot j_{\ell'}(k's) .$$

III. Results

SDSS-BOSS data analysis results

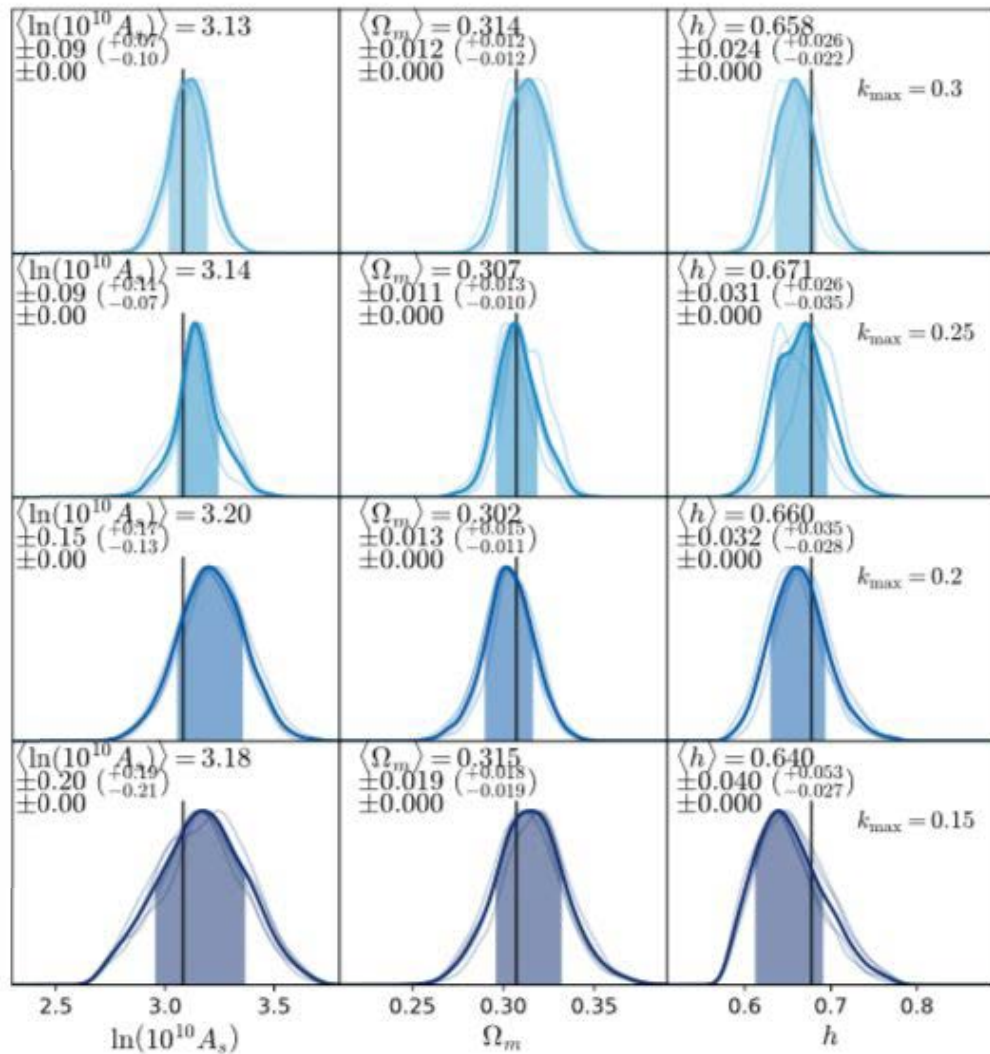
Tests against simulations

SDSS ‘challenge’ boxes

~ 4 times the effective volume of
SDSS-BOSS CMASS sample

No theory-systematics detected
within 1-sigma statistical fluctuations
of the simulation

Error bars shrinking with k_{\max}



Application of CMB sound horizon prior



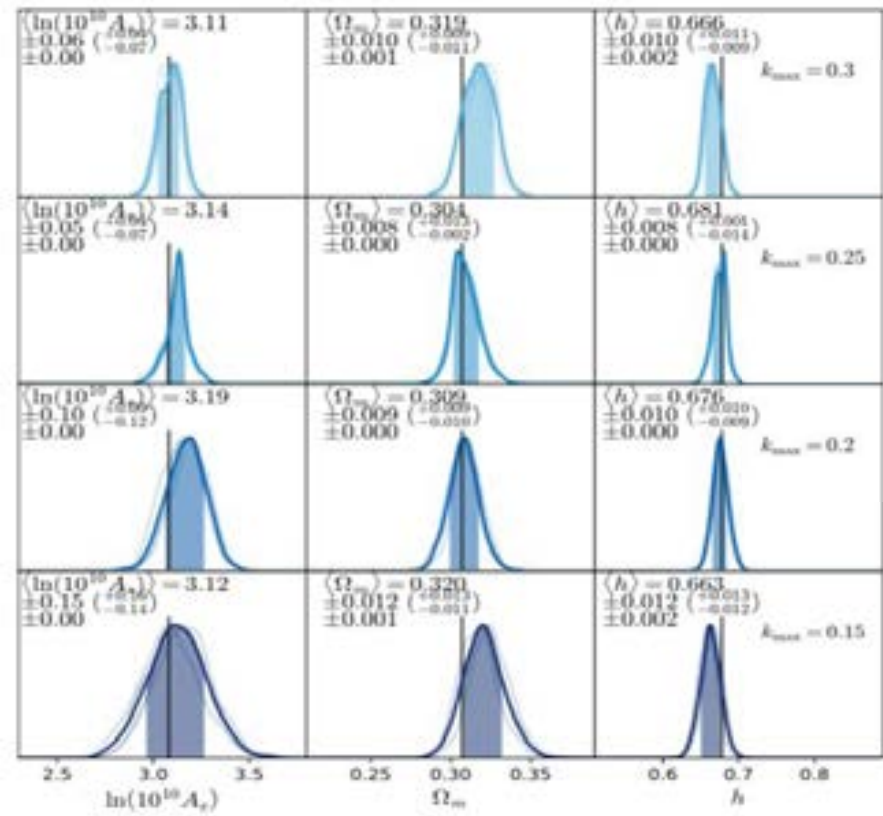
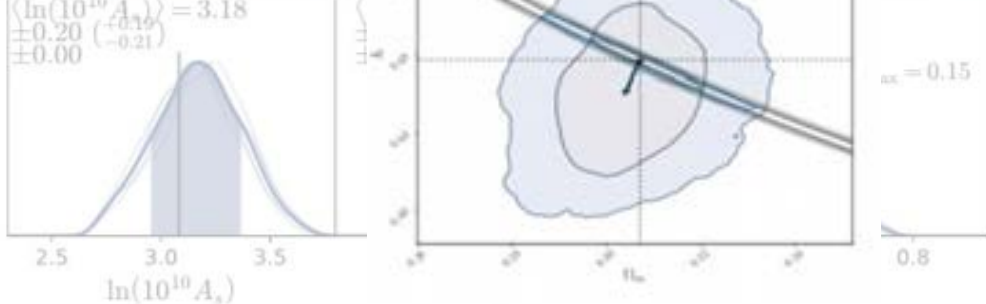
$$r_d = \int_{z_d}^{\infty} \frac{c_s(z)}{H(z)} dz, \quad c_s^2(z) = \frac{c^2}{3} \left[1 + \frac{3 \rho_b(z)}{4 \rho_\gamma(z)} \right]^{-1}$$



Reduction of statistical errors
 $\sim \{35, 20, 62\} \%$



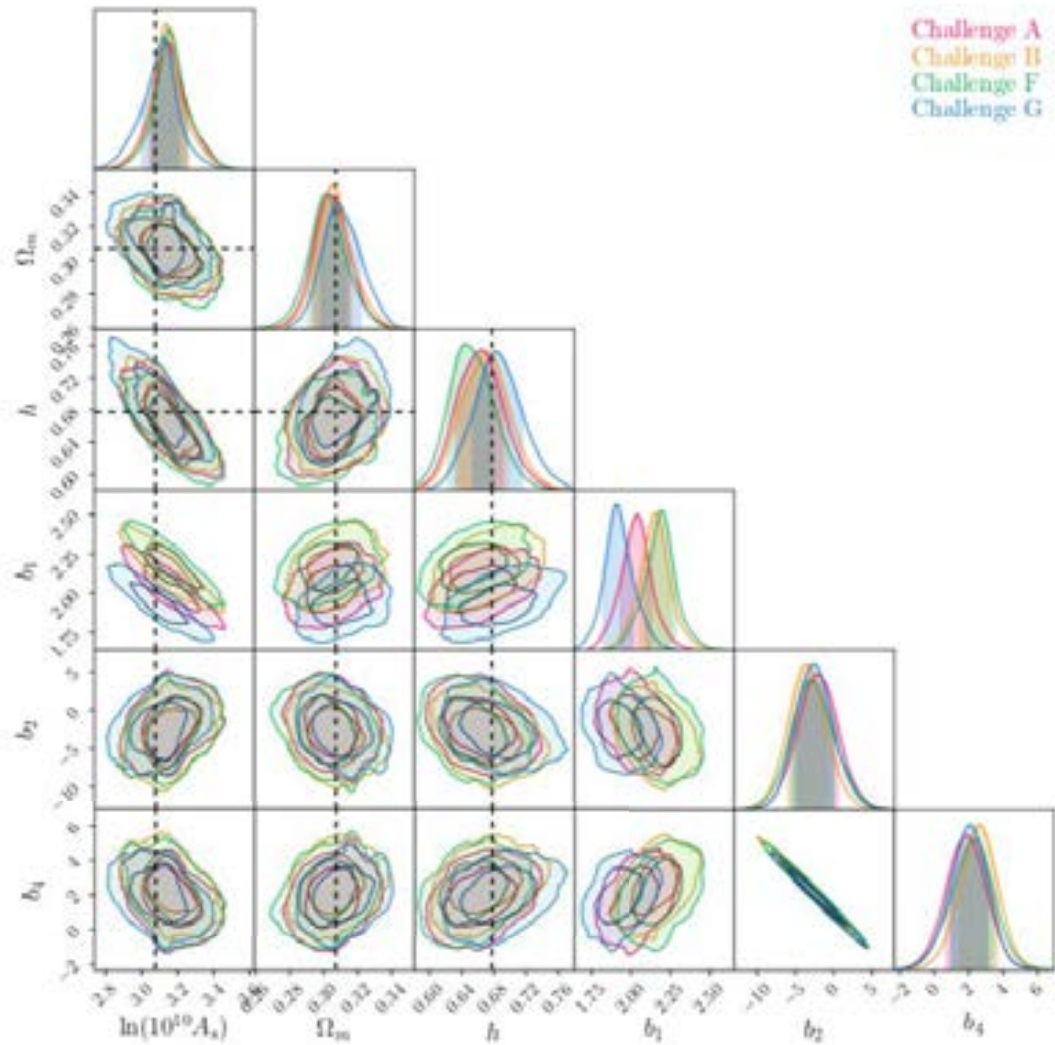
Theory-systematic errors decreased



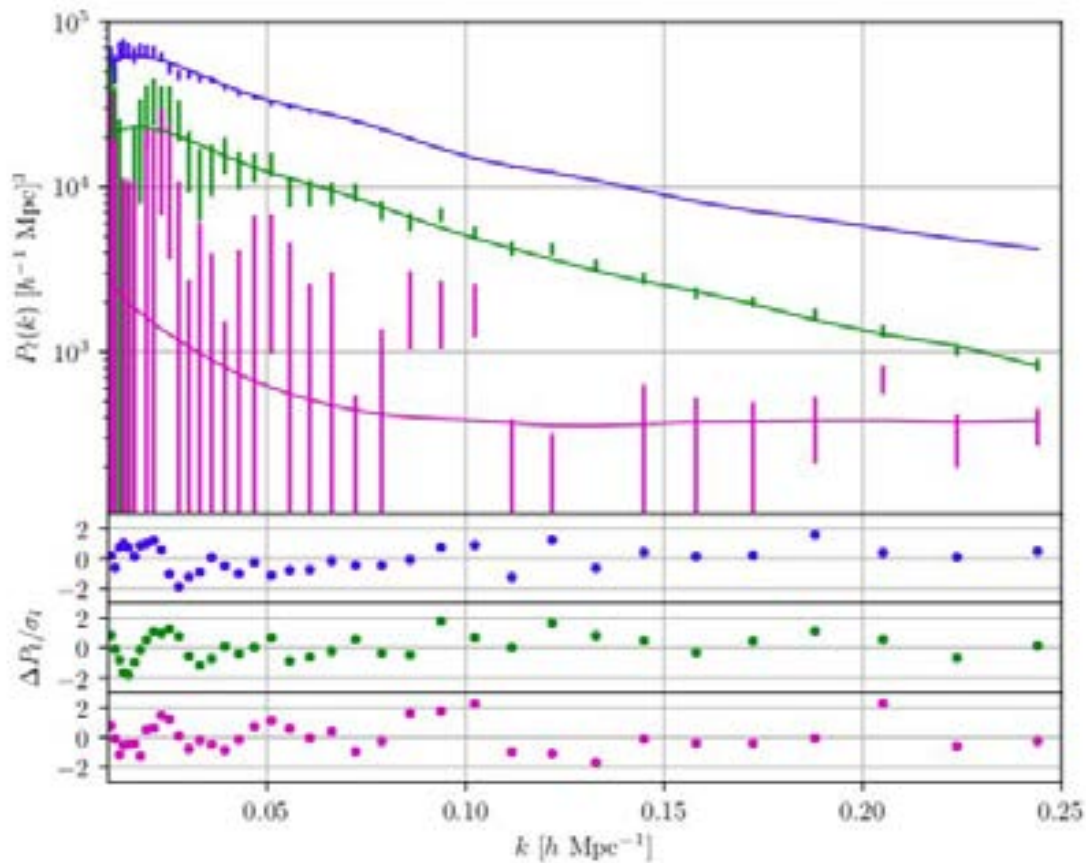
Tests against simulations

Contour plot

Different HOD models differ on linear bias b_1



SDSS-BOSS NGC CMASS



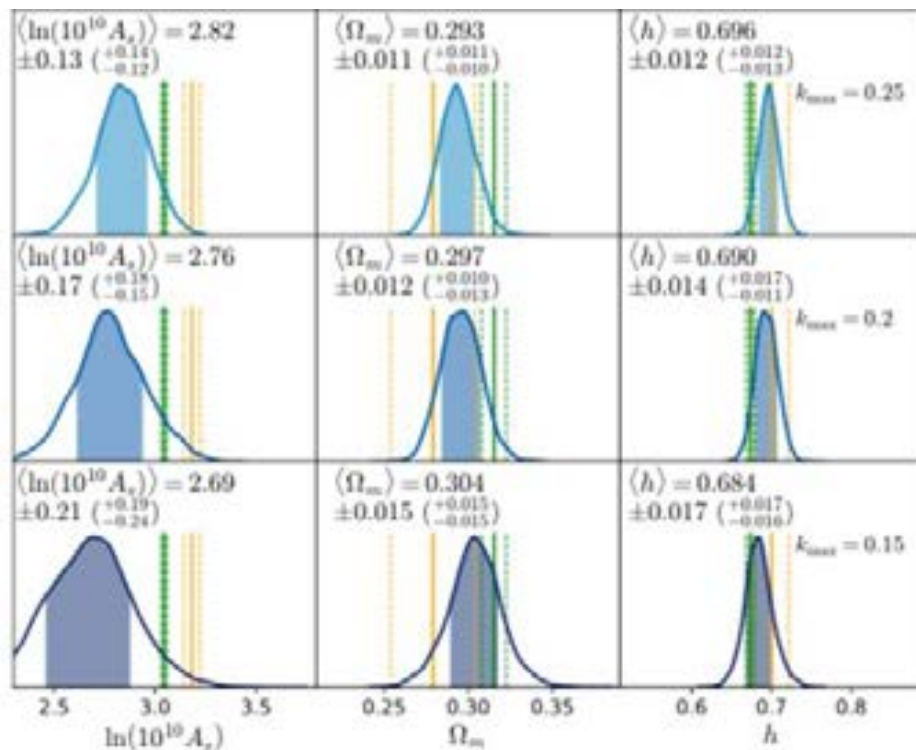
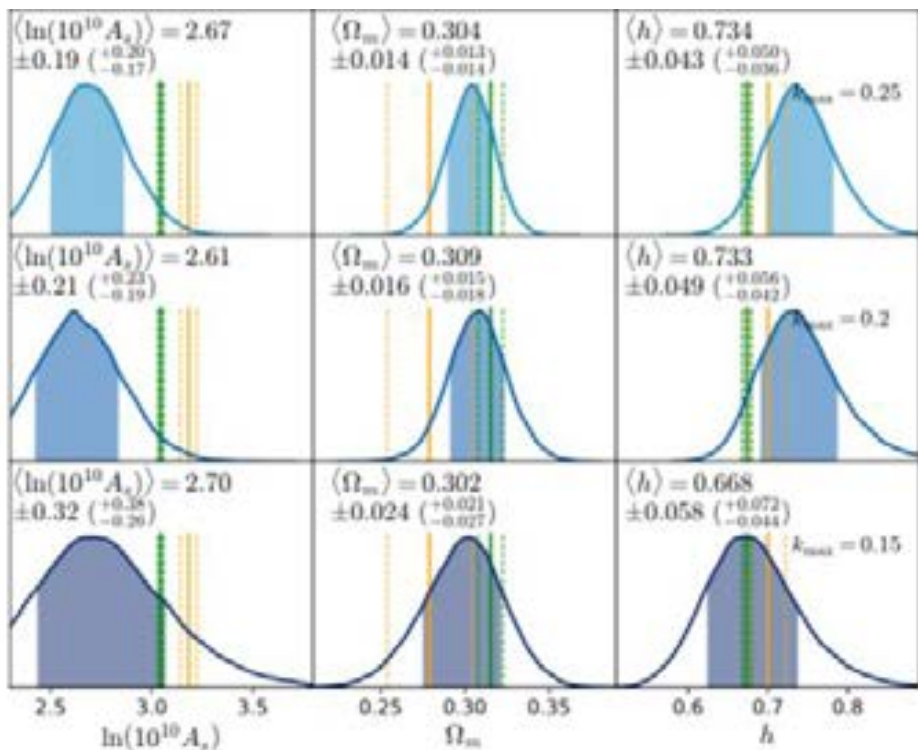
min $\chi^2/\text{d.o.f.}$ $\sim 106/100$

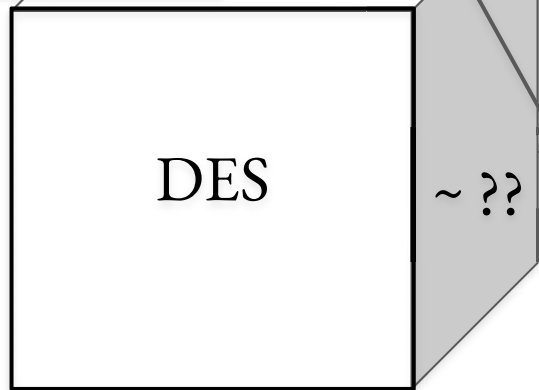
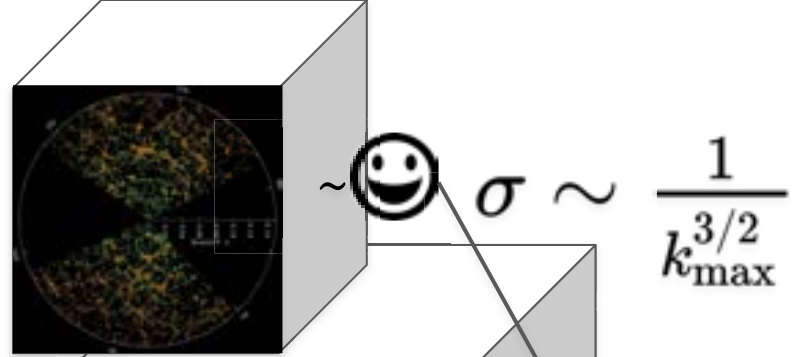
p-value: 0.32

SDSS-BOSS NGC CMASS

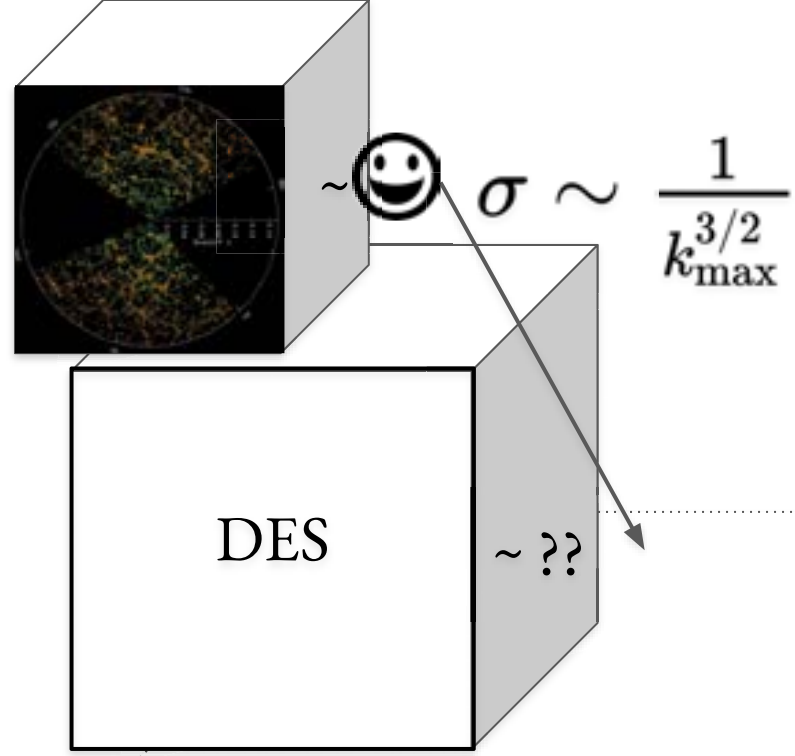
$\{A_s, \Omega_m, h\}$ measured $\sim 15\%, 5\%, 5\%$

with CMB sound horizon prior:
14%, 3.8% and 1.9%





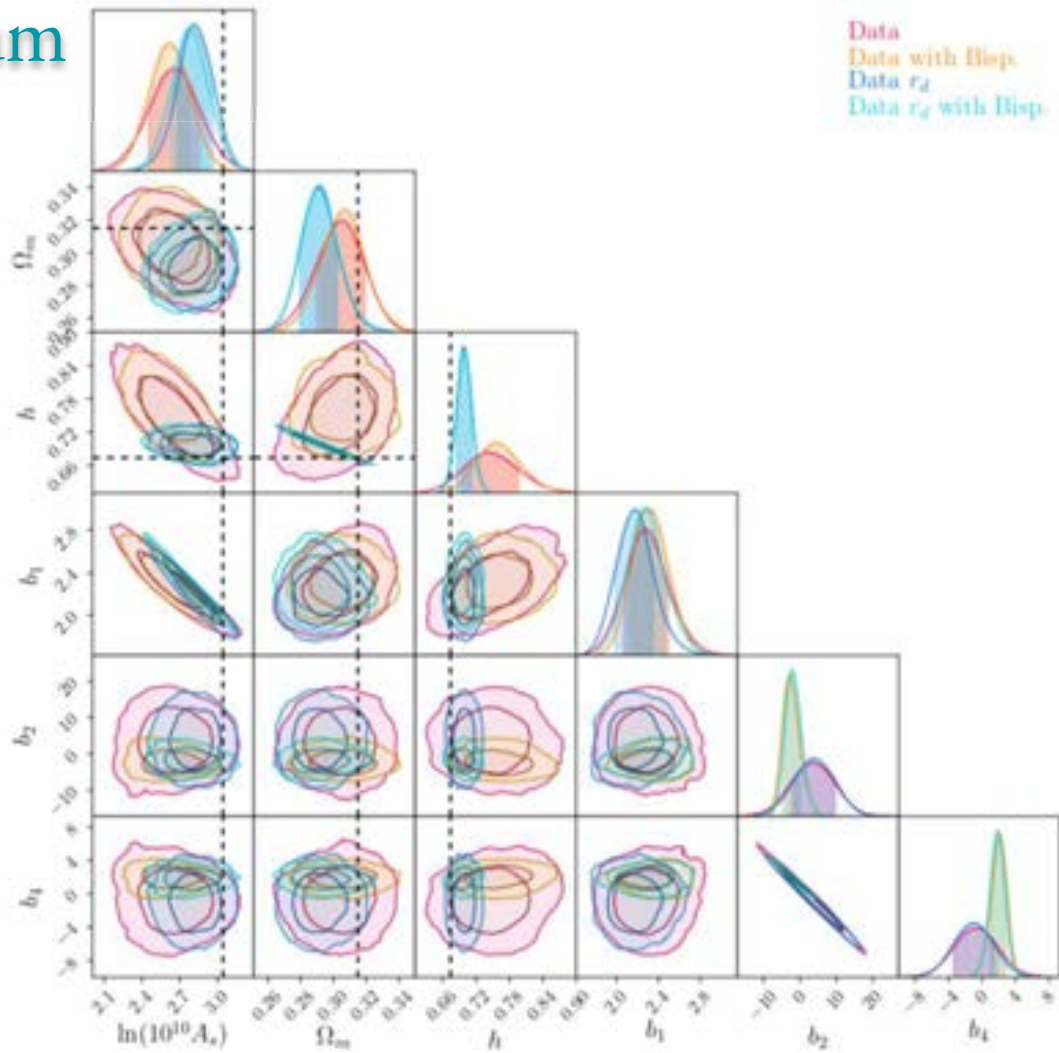
Euclid, ...



Thanks for your attention !

Euclid, ...

Inclusion of the bispectrum



Last two-decades approach: BAO extraction and RSD

Baryon Acoustic Oscillations Redshift-Space Distortions

BAO extraction: ‘wiggle’ - ‘non-wiggle’ separation

> broad-band signal not analyzed

> non-smooth features in the primordial spectrum missed

> degeneracy $H_0 - \Omega_m$

RSD > degeneracy $f\sigma_8$

> Input from either CMB (‘inverse-cosmic ladder’) or SNe (‘cosmic ladder’)

necessary to break degeneracies

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necessary to break degeneracies *

Non-independent
measurements

Information loss

Introduction
of systematics

No probe of
baryons-to-matter
fraction, etc.

*To be totally fair: redshift tomographic measurements also can do

Can we do better with the EFTofLSS?